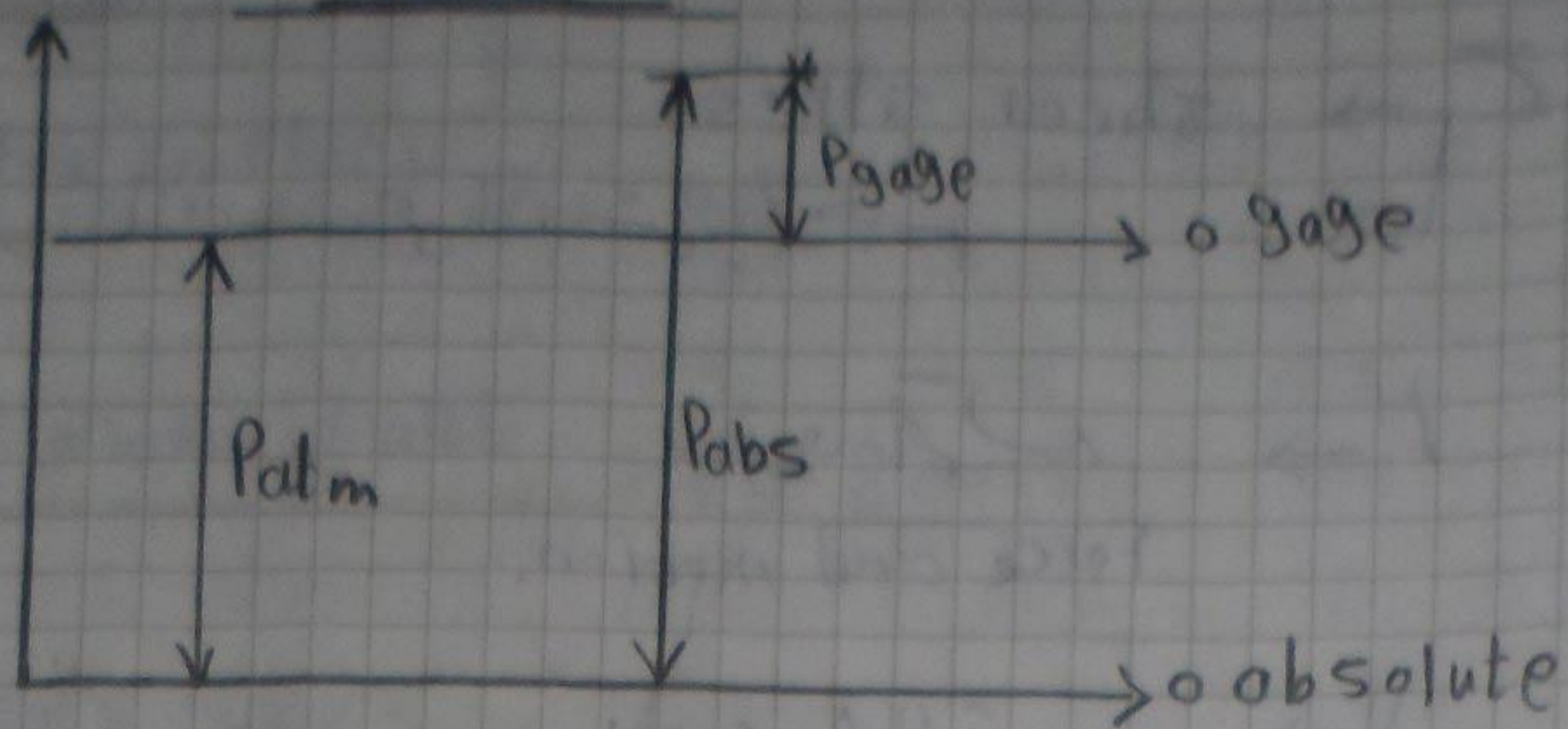


# Sheet No. 2

III

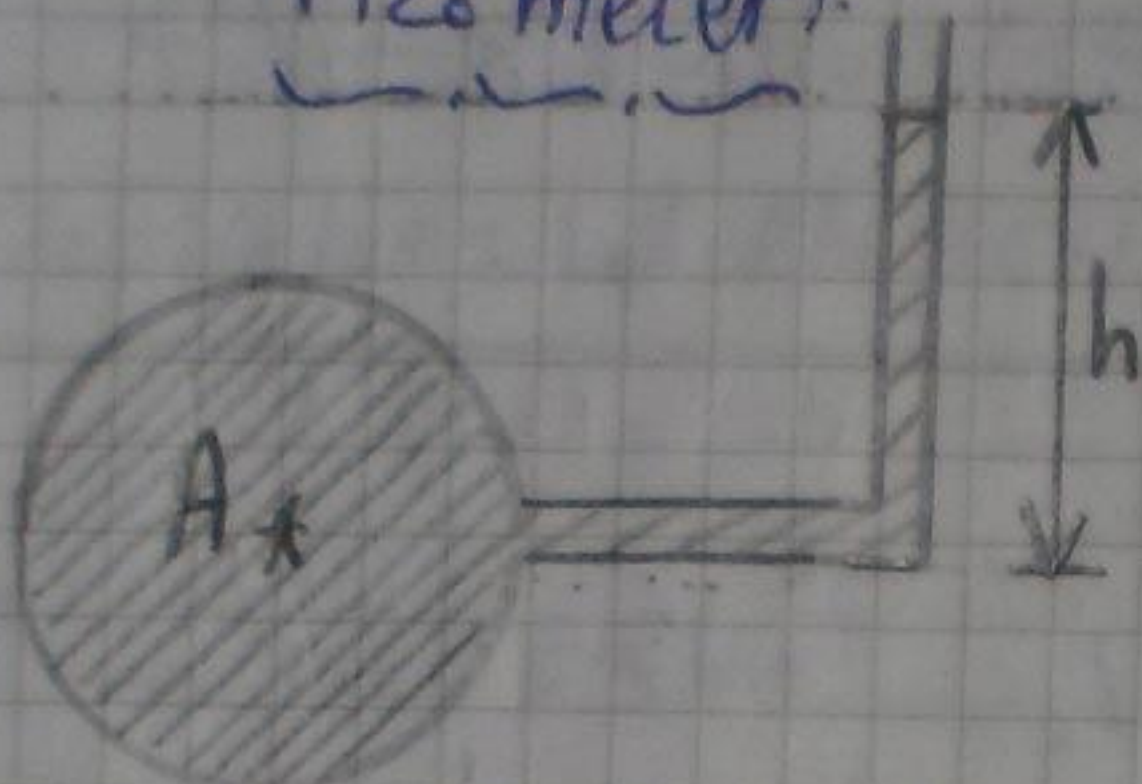
(a)

$$P_{abs} = P_{gage} + P_{atm}$$



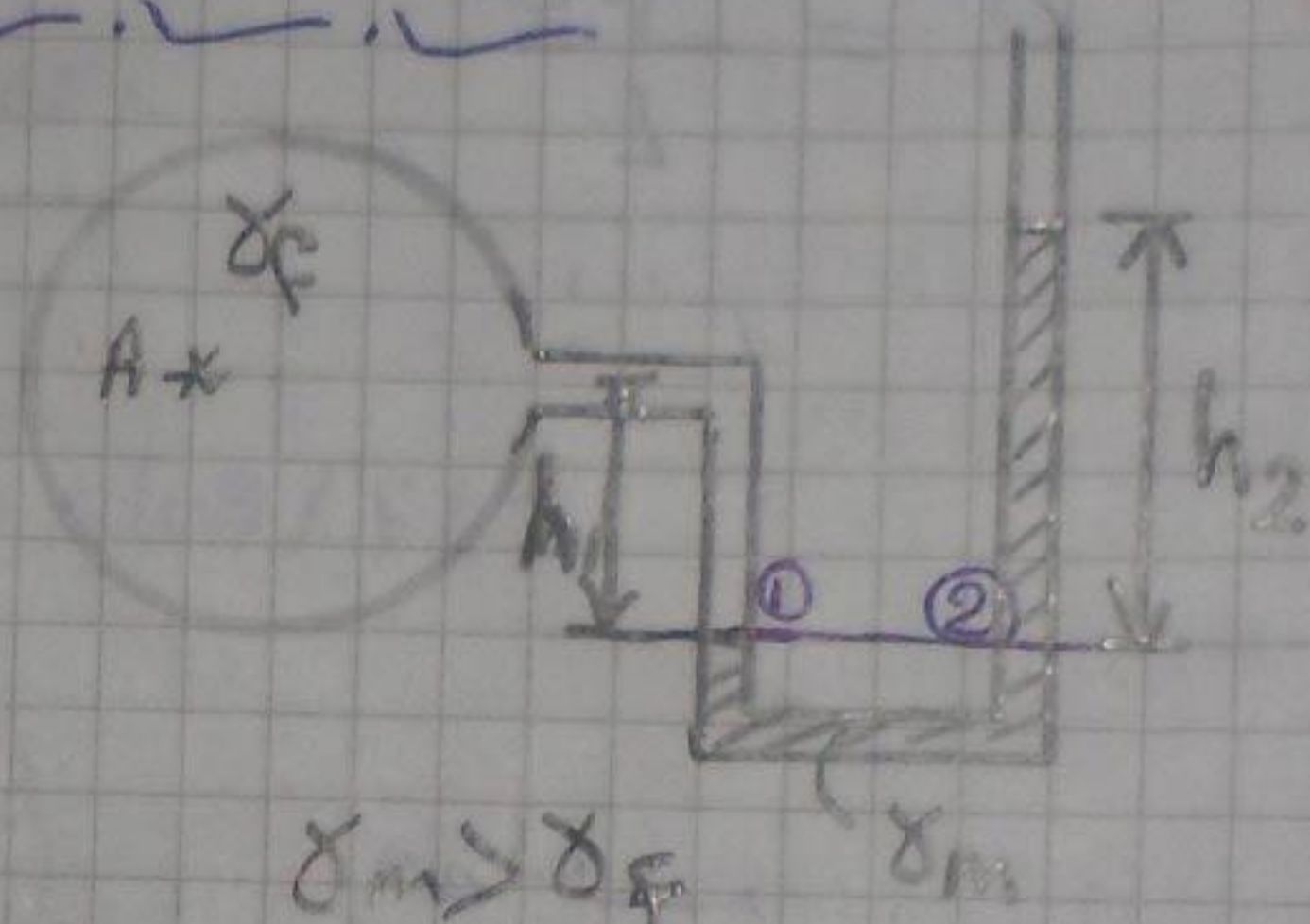
(b)

Piezometer:



measures +ve gage pressures of low magnitudes

Manometer:



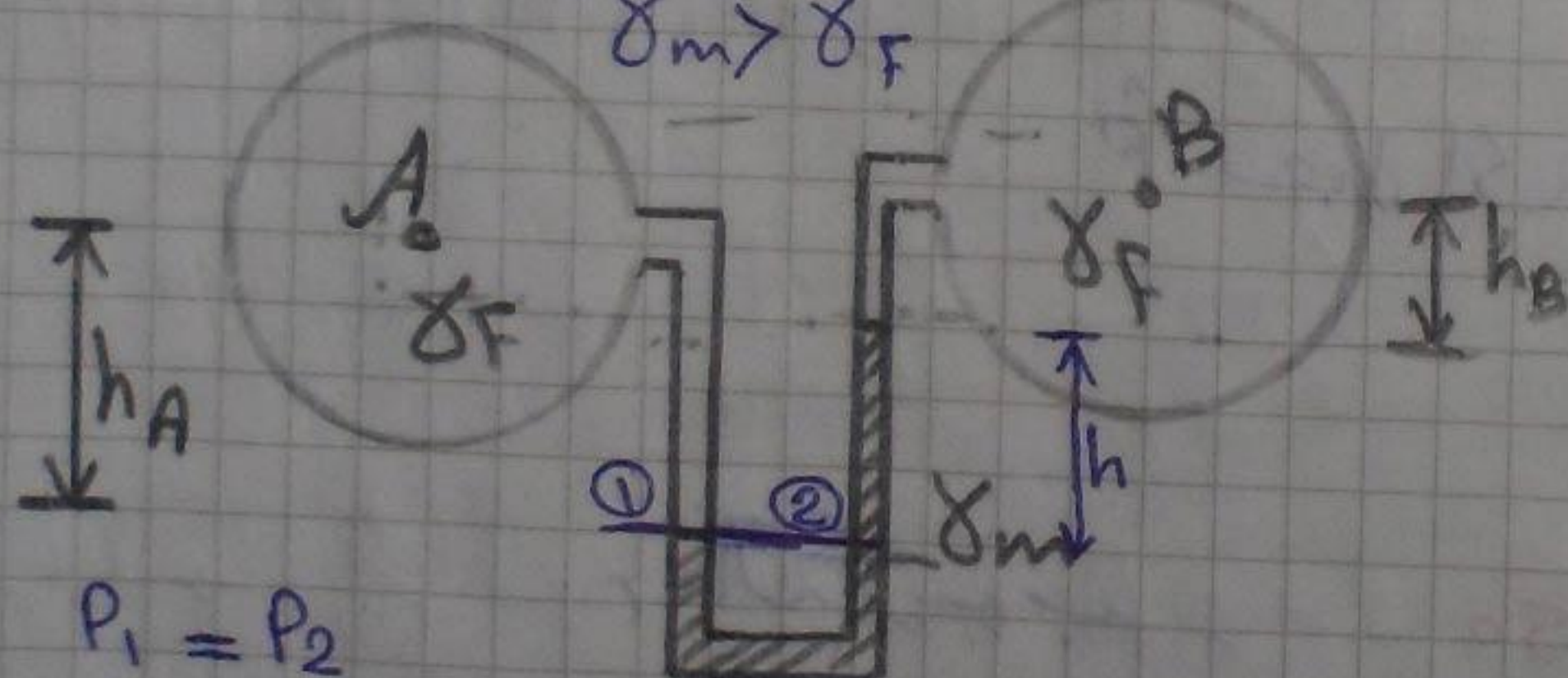
$$\gamma_m > \gamma_f$$

$$P_1 = P_2$$

$$P_{gage} = \gamma_m h_2 - \gamma_f h_1$$

differential manometer:

$$\gamma_m > \gamma_f$$



$$P_1 = P_2$$

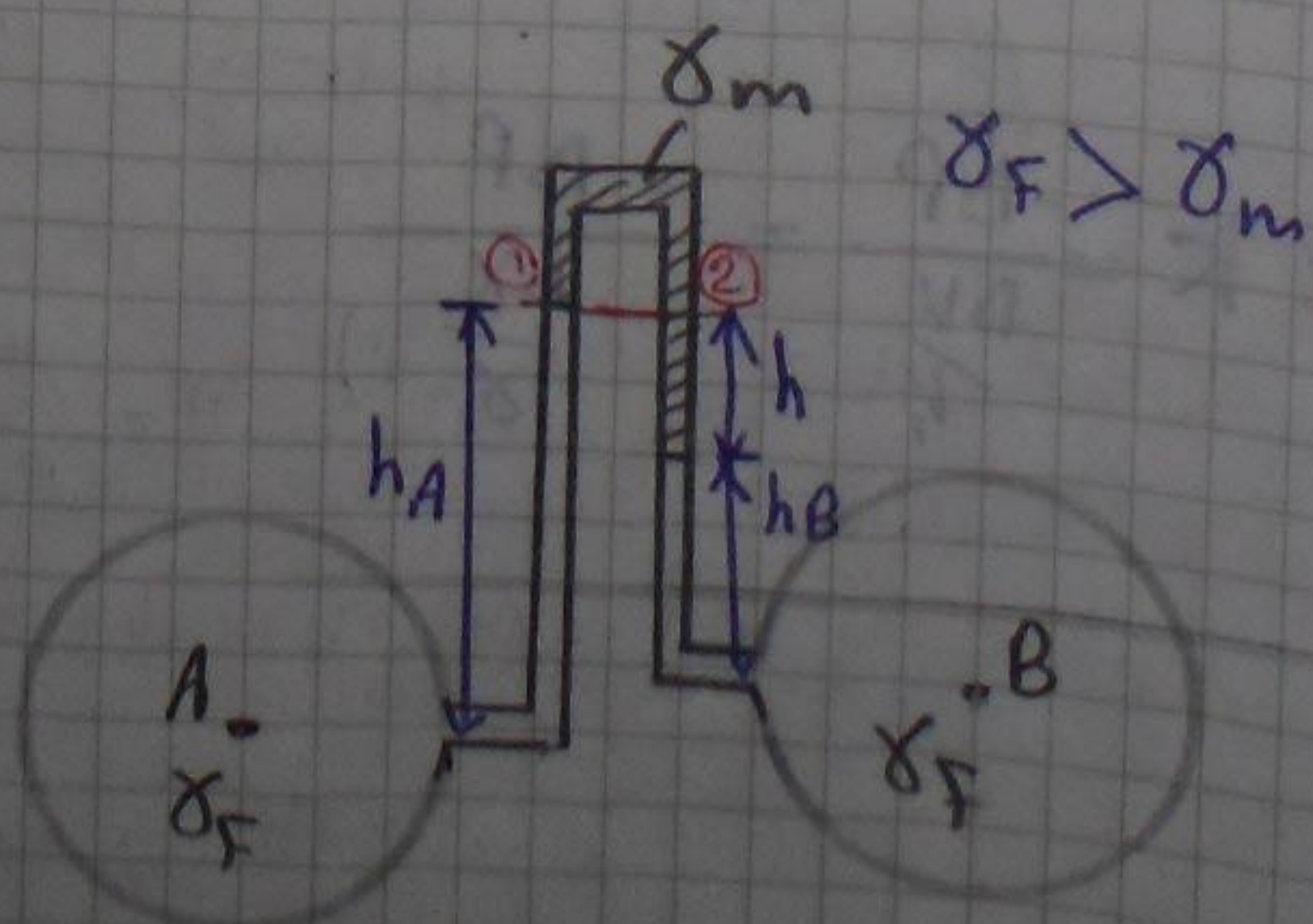
$$P_A = -\gamma_f h_A \quad \& \quad P_B = -\gamma_f h_B - \gamma_m h$$

$$P_A - P_B = -\gamma_f h_A + \gamma_f h_B + \gamma_m h$$

$$P_1 = P_2$$

$$P_A = \gamma_f h_A \quad , \quad P_B = \gamma_f h_B + \gamma_m h$$

$$P_A - P_B = \gamma_f h_A - \gamma_f h_B - \gamma_m h$$

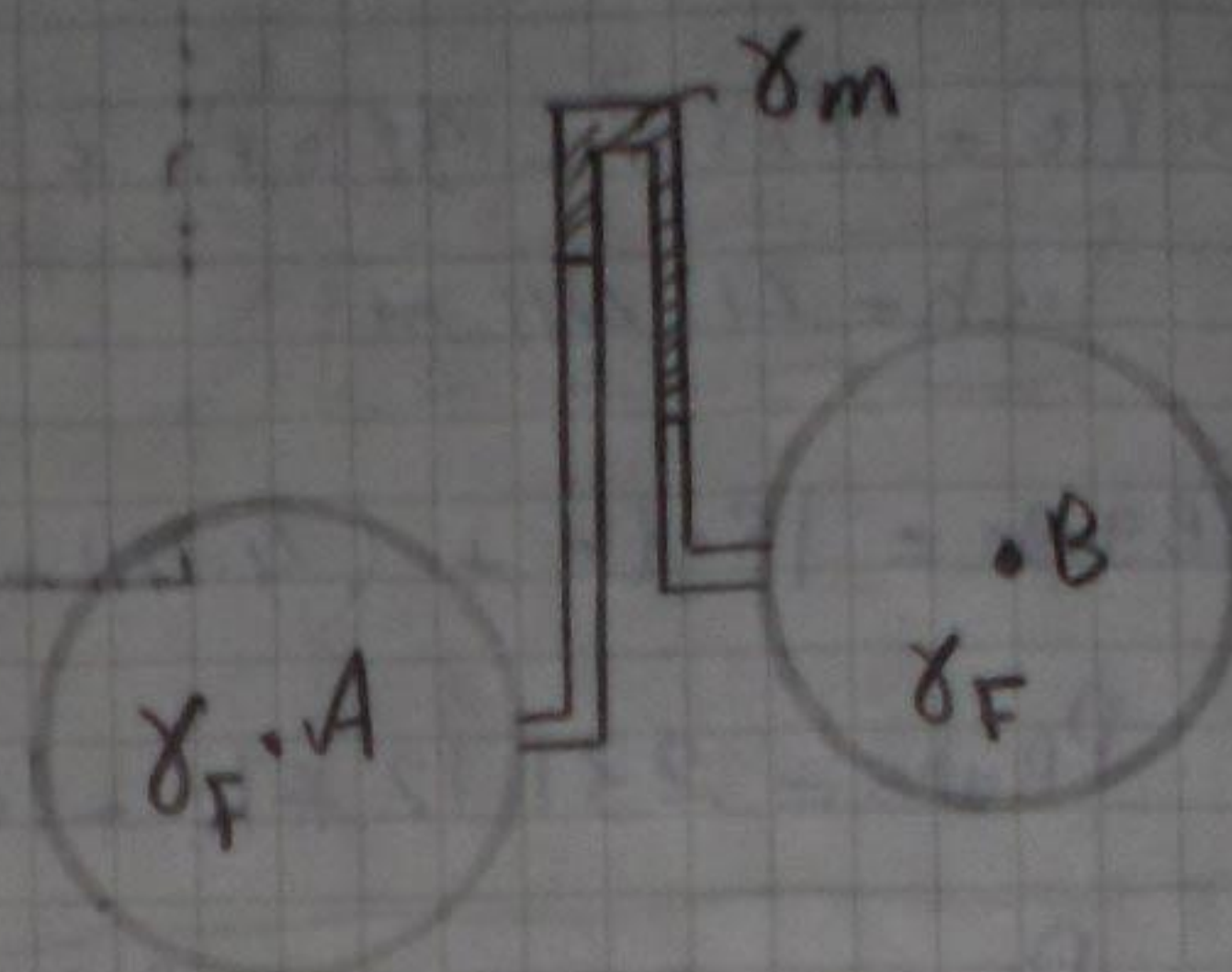




- (c) ① Can't measure (-ve) gauge pressure.  
 ② measure Pressure only of low magnitudes.

(d) using lighter fluid

$$\gamma_F > \gamma_m$$



(2) (1)  $P = 1.75 \text{ kgw/cm}^2 = \frac{1.75 \times 9.81}{10^{-4}} = 171675 \text{ N/m}^2$

(2)  $171675 = 9810 \times h_w \quad \Rightarrow \quad h_w = 17.5 \text{ m}$

(2)  $\gamma = 0.85 \times 9810 = 8338.5 \text{ N/m}^3$

$h_{oil} = \frac{171675}{8338.5} \quad \Rightarrow \quad h_{oil} = 20.59 \text{ m}$

(3)  $\gamma = 13.6 \times 9810 = 133416 \text{ N/m}^3$

$h_{Hg} = \frac{171675}{133416} \quad \Rightarrow \quad h_{Hg} = 1.28 \text{ m} = 128 \text{ cm}$

(b)  $h_w = 12 \text{ m}$

(1)  $P = 12 \times 9810 \quad \Rightarrow \quad P = 117720 \text{ N/m}^2$   
 $1 \text{ lb} = 4.44 \text{ N} \quad \text{inch} = 0.0254 \text{ m}$

$\Rightarrow P = \frac{(117720)(0.0254)^2}{(4.44)} \quad \Rightarrow \quad P = \frac{17.105}{4.44} \text{ lb/in}^2$

(2)  $h_{Hg} = \frac{117720}{13.6(9810)} \quad \Rightarrow \quad h_{Hg} = 0.88 \text{ m} \quad \Rightarrow \quad h_{Hg} = 88 \text{ cm}$



h = ?  $P_{Babs} = ?$

$P_{Agage} = 330 \times 10^3 \text{ N/m}^2$

$P_{Agage} = P_{air} + \gamma_w h + \gamma_{Hg} \times 0.8$

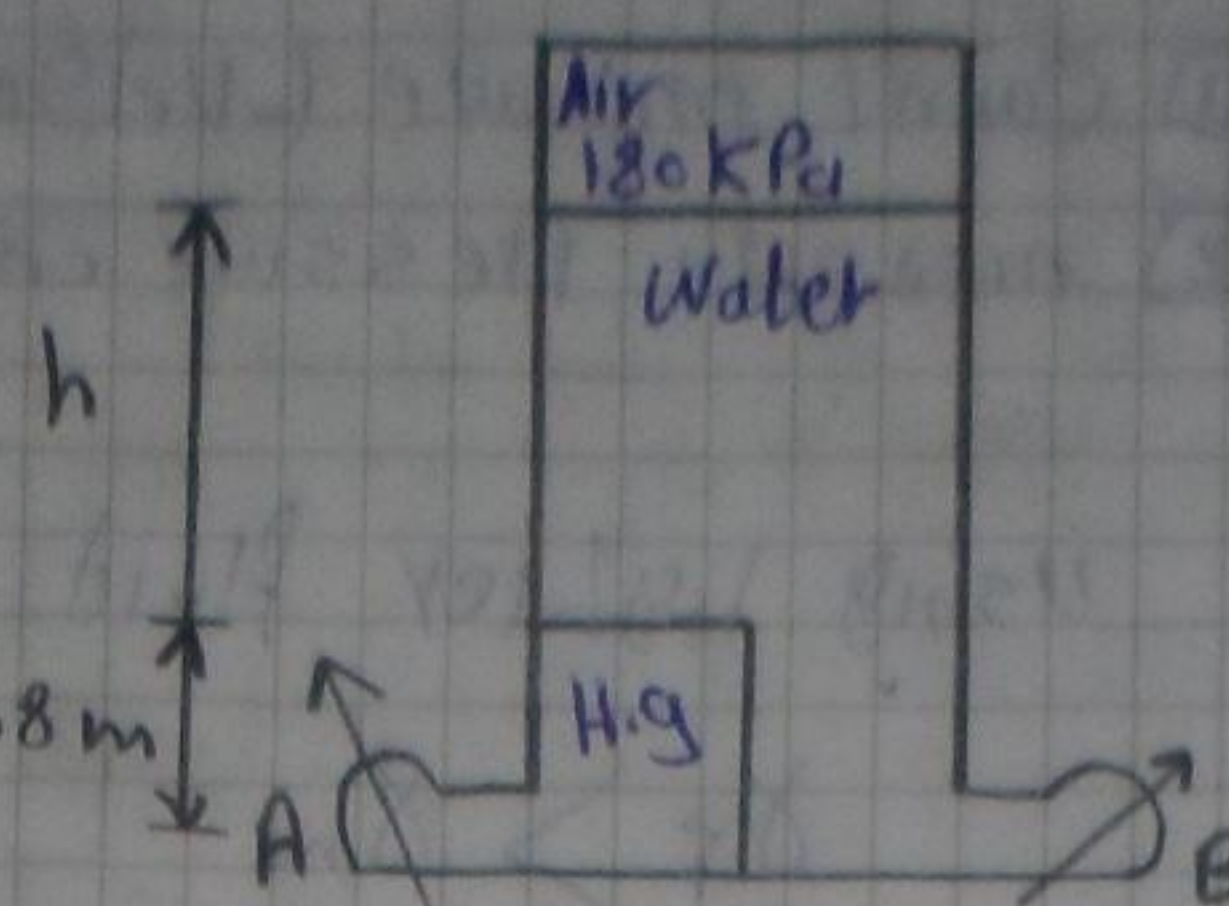
$330 \times 10^3 = 180 \times 10^3 + 9810 \times h + 13600 \times 9.81 \times 0.8$

$\therefore h = 4.411 \text{ m}$

$P_{Bgage} = 180 \times 10^3 + (4.411 + 0.8) 9810$

$P_{Babs} = 231.12 \times 10^3 + 101.3 \times 10^3$

$\therefore P_{Babs} = 332.42 \text{ kPa}$



$\therefore P_{Bgage} \leq 231.12 \text{ kPa}$

④

$h = -0.225 \text{ m}$

$\gamma_{Hg} = 13600 \times 9.81$

$P_A = P_i \gamma (h + 1.9)$

$P_A = \gamma_w (h + 1.9) + 0.197 \times 10^5$

$P_i = \gamma_{Hg} h + \gamma_{oil} (36.1 - 32.2) - 30552.264$

$\therefore 9810 (h + 1.9) + 0.197 \times 10^5 = 1.6 \times 9810 h + 0.9 \times 9810$

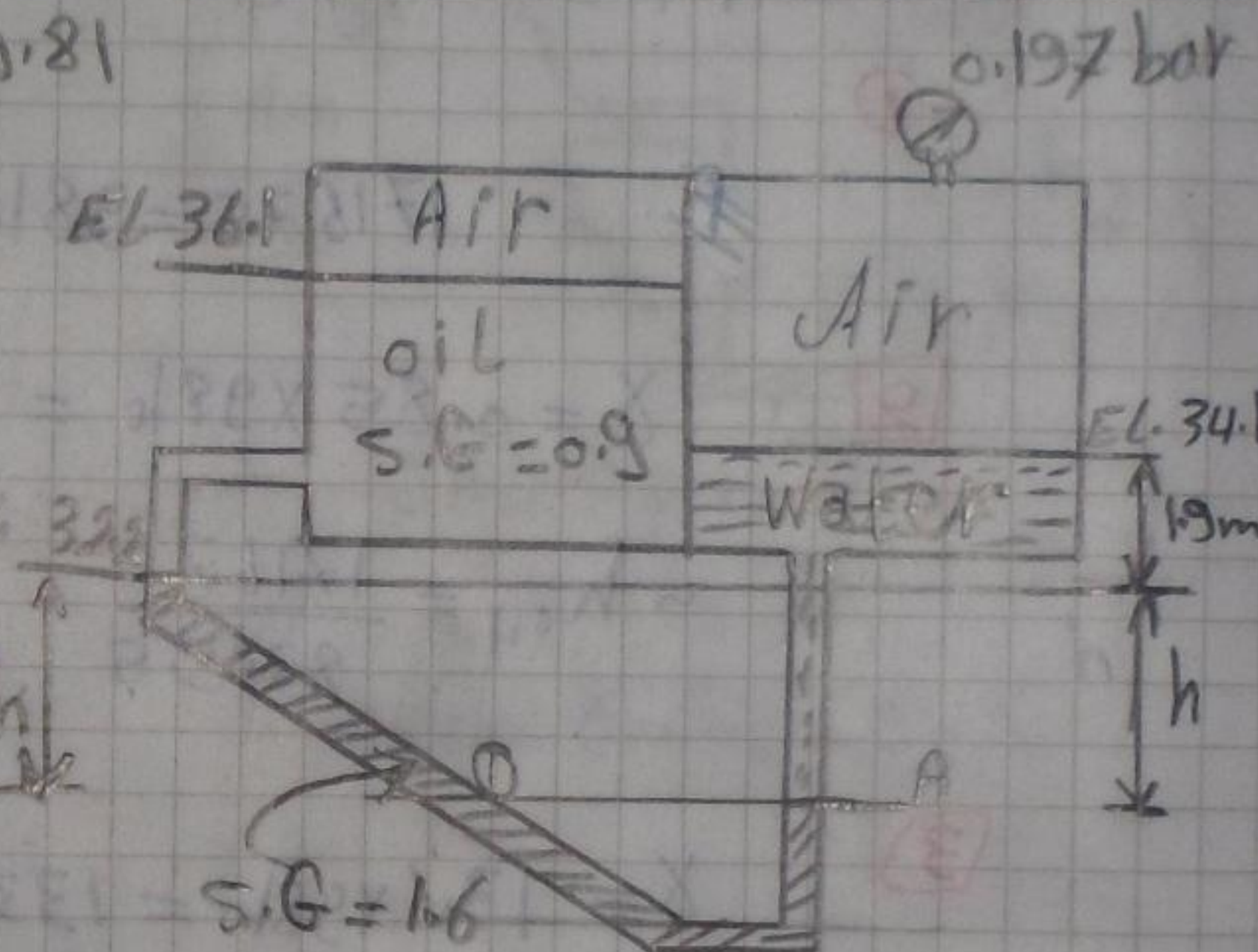
$\therefore 9810 h - 1.6 \times 9810 h = 9810 \times 1.9 - 15819.104$

$-5886 h = -34458.104$

$\therefore h = 5.85 \text{ m}$

$\therefore E.L. A = 34.1 - 1.9 - 5.85$

$\therefore E.L. A = 26.35$



⑤

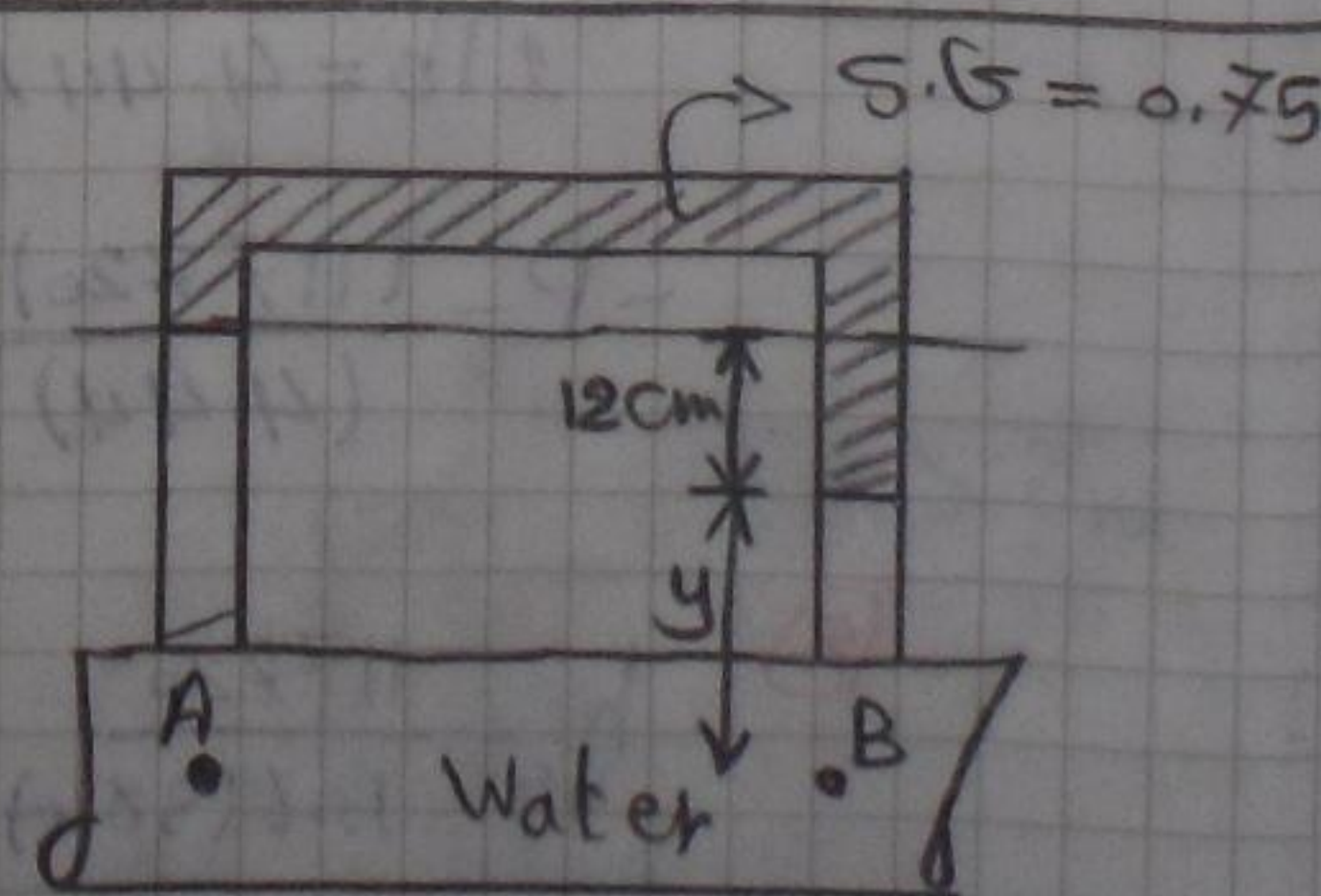
$P_A = \gamma_w (y + 0.12) = \gamma_w y + 12 \gamma_w$

$P_B = \gamma_w y + 0.12 (0.75 \times 9810)$

$P_A - P_B = 12 (9810) - 12 \times 0.75 \times 9810$

$\therefore P_A - P_B = 29430 \text{ Pascal}$

$\therefore P_A - P_B = 2.943 \times 10^{-3} \text{ bar}$



1 bar  $\rightarrow 10^5 \text{ Pascal}$

2 bar  $\rightarrow 294.30$



⑥ a)  $P_A - P_B = ?$  oil

$P_1 = P_2$  &  $P_3 = P_4$  &  $P_5 = P_6$

$P_1 = (13600 \times 9.81)(30 \times 0.0254)$  ①

$+ (9810)(10 \times 0.0254) + P_B$

$P_2 = P_3 + (0.8 \times 9810)(18 \times 0.0254)$  ②

$P_6 = (9810)(66 \times 0.0254) + P_A$  ③

$P_5 = (13600 \times 9.81)(40 \times 0.0254) + P_4$  ④

①, ③

~~$1 + 10 + 662.992 + 2491.74 + P_B = 16445.48 + P_A - P_6$~~

~~$P_A - P_B$~~   $P_1 = P_2$

$\therefore 104154.732 + P_B = P_3 + 3588.1056$  ⑤

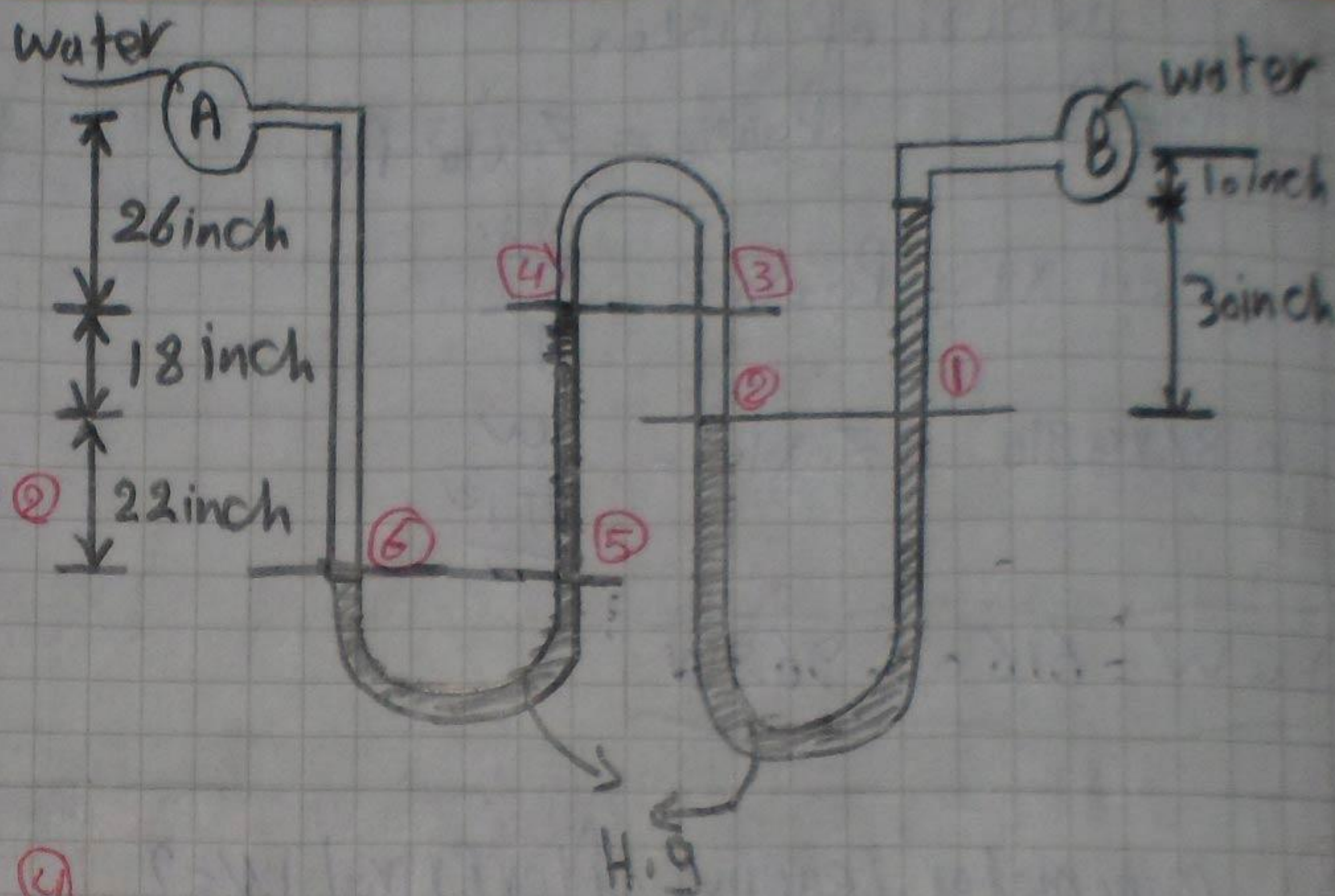
$P_5 = P_6$

$135550.656 + P_A = 16445.48 + P_A$  ⑥

$\therefore P_3 = P_A$  and soln ⑤, ⑥

~~$\therefore P_3 - P_B - 100566.6264 = -P_A + P_A + 119105.172$~~

$P_A - P_B = 219671.7984 \text{ N/m}^2$



⑥ b)

Air



⑥⑧

Air

$$P_1 = P_2, \quad \cancel{P_3} + P_3 = P_4, \quad P_5 = P_6$$

$$P_1 = 13600 \times 9.81 \times 30 \times 0.0254 + 9810 \times 16 \times 0.0254 + P_B$$

$$\therefore P_1 = 104154.732 + P_B \rightarrow \textcircled{1}$$

$$\cancel{P_2 = P_2} \quad P_2 = P_3 \rightarrow \textcircled{2}$$

$$P_6 = 9810 \times 66 \times 0.0254 + P_A$$

$$\therefore P_6 = 16445.484 + P_A \rightarrow \textcircled{3}$$

$$P_5 = 13600 \times 9.81 \times 40 \times 0.0254 + P_4$$

$$\therefore P_5 = 135550.656 + P_4 \rightarrow \textcircled{4}$$

$$\therefore P_1 = P_2 = P_3 = P_4$$

$$104154.732 + P_B = P_3 \rightarrow \textcircled{5}$$

$$16445.484 + P_A = 135550.656 + P_4 \rightarrow \textcircled{6}$$

$$\therefore P_3 = P_4$$

$$\therefore \cancel{P_3} - 104154.732 - P_B = 135550.656 + \cancel{P_4} - 16445.484 - P_A$$

$$\therefore P_A - P_B = 223259.904 \text{ N/m}^2$$

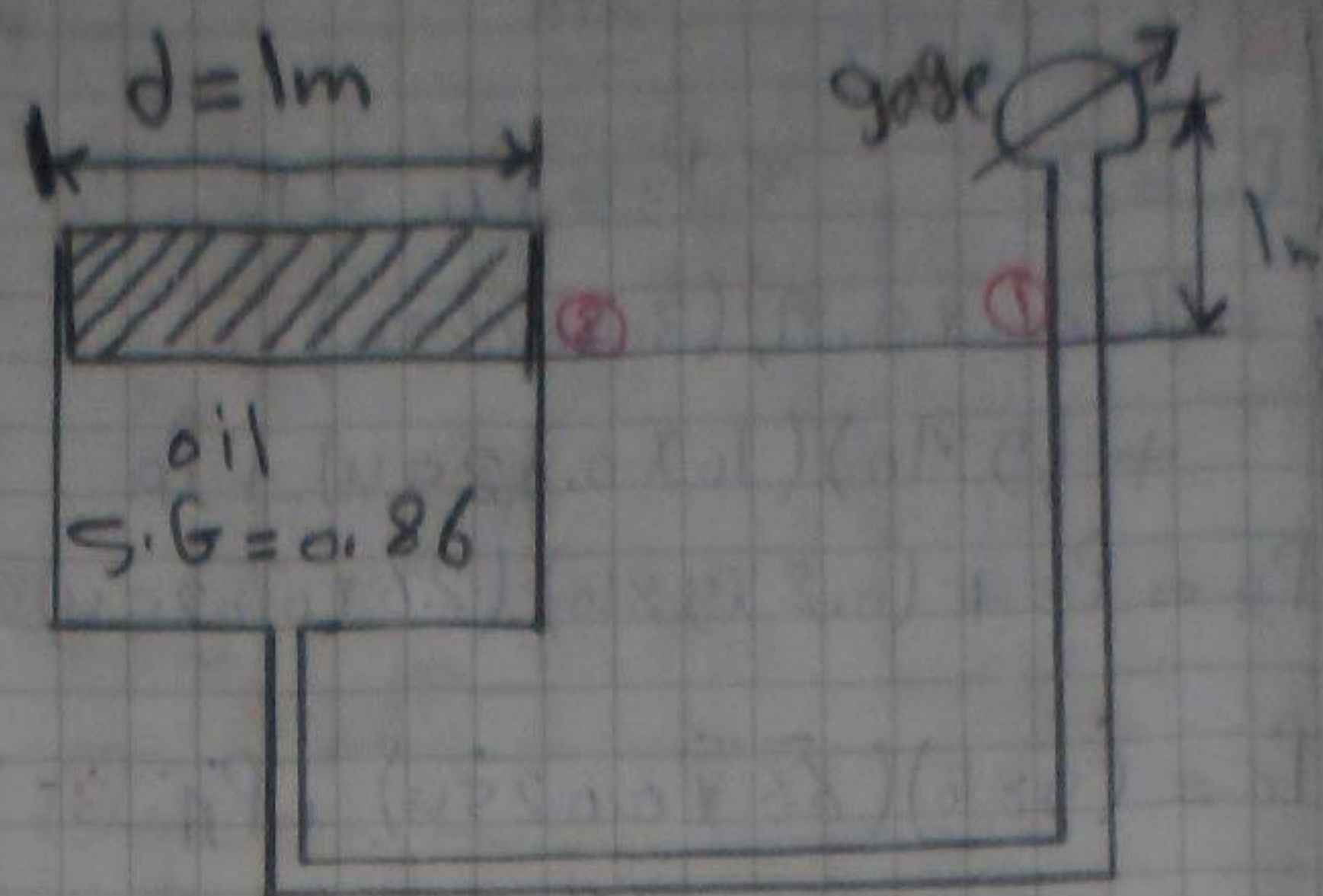


Weight of piston  
 $P_1 = P_2$        $P_{gase} = 70 \times 10^3 \text{ Pa}$

$$\gamma_{oil} \times 1 + P_{gase} = \frac{W}{A}$$

$$0.86 \times 9810 + 70 \times 10^3 = \frac{W}{\frac{\pi 1^2}{4}}$$

$$\therefore W = 61603.962 \text{ N}$$



⑧ manometer reading after Extra 1N = ?

$$P_1 = P_2$$

$$\gamma_{H.g} (0.075) = \gamma_{oil} (0.6) + P_{pan} \frac{W}{A}$$

$$13600 \times 9.81 \times 0.075 = 0.92 (9810) (0.6) + \frac{W}{\frac{\pi 0.05^2}{4}}$$

$$\therefore W = 9.01 \text{ N}$$

after loading

$$W = 10.01 \text{ N}$$

$$P_3 = P_4$$

$$\gamma_{H.g} (0.075 + 2h) = \gamma_{oil} (0.6 + h - y) + \frac{W}{A}$$

$$\therefore 25^2 = 625 \quad \therefore 50^2 = 2500$$

$$\therefore \frac{2500}{625} = 4$$

$$\therefore y = 4h$$

$$\therefore 13600 \times 9.81 (0.075 + 2h) = 0.92 (9810) (0.6 + h - 4h) + \frac{10.01}{1.9 \times 10^{-4}}$$

$$10006.2 + 266832h = 5415.12 - 27075h + 5268.421$$

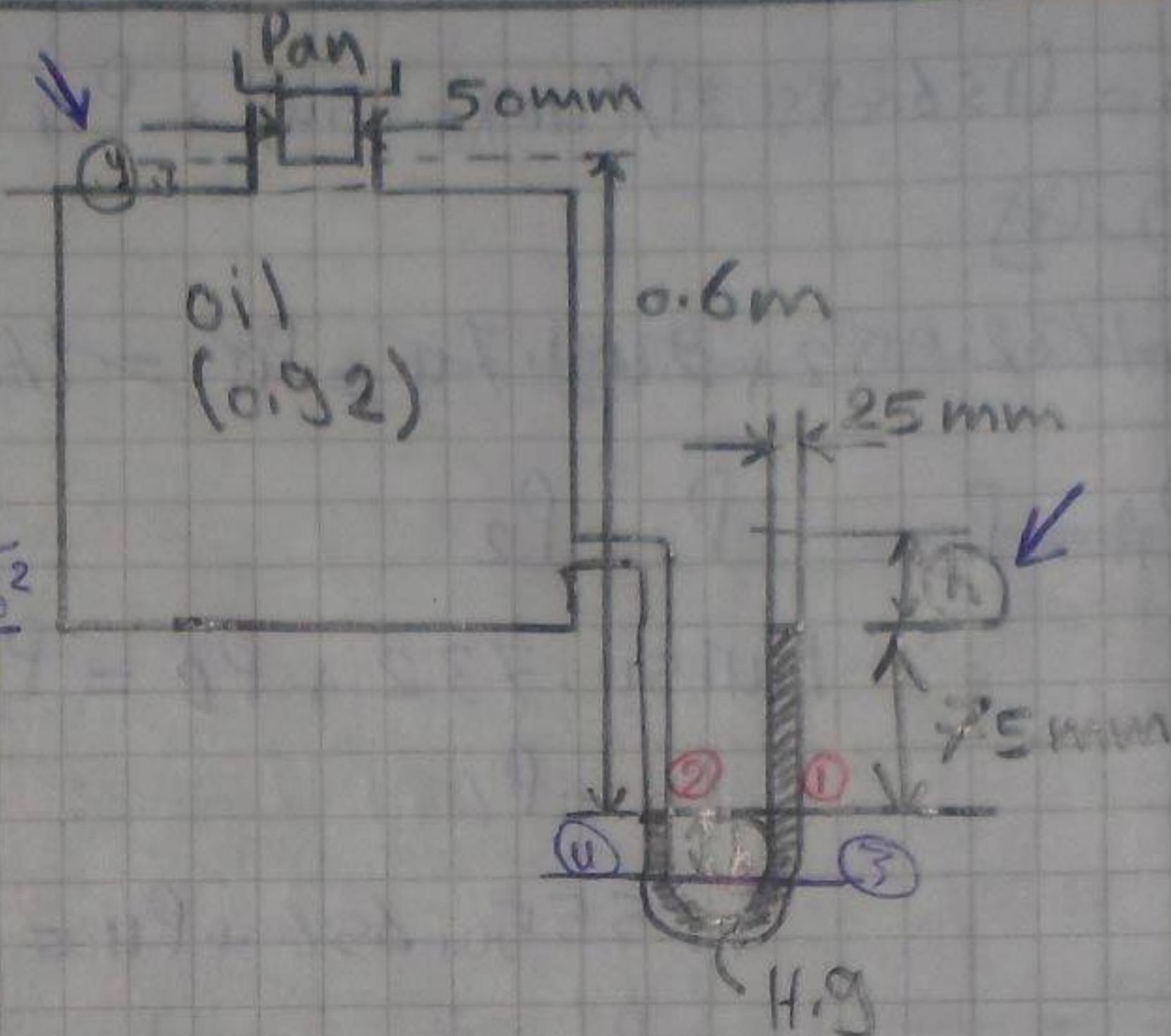
$$293907h = 677.341$$

$$= 2.305 \times 10^{-3} \text{ m}$$

$$\therefore h = 2.305 \text{ mm}$$

$$\rightarrow h + 75 \text{ mm}$$

$$\therefore \text{manometer reading after Extra 1N} = 77.3 \text{ mm}$$





9

$$S.G_{oil} = ?$$

$$A/a = 50 \leftarrow$$

$$P = ?$$

$$D = 3 \text{ cm}$$

$$P_1 = P_2$$

$$\gamma_{oil} (0.255) = \gamma_w (0.21)$$

$$\gamma_{oil} (0.255) = 9810 (0.21)$$

$$\therefore \gamma_{oil} = 8078.824 \text{ N/m}^3$$

$$S.G_{oil} = \frac{\gamma_{oil}}{\gamma_w} = \frac{8078.824}{9810}$$

$$\therefore S.G_{oil} = 0.824$$

after loading:-

$$\Delta \text{Volume} = \text{Constant}$$

$$Ay = a\Delta$$

50

$$(50 \text{ g}) y = a (0.03)$$

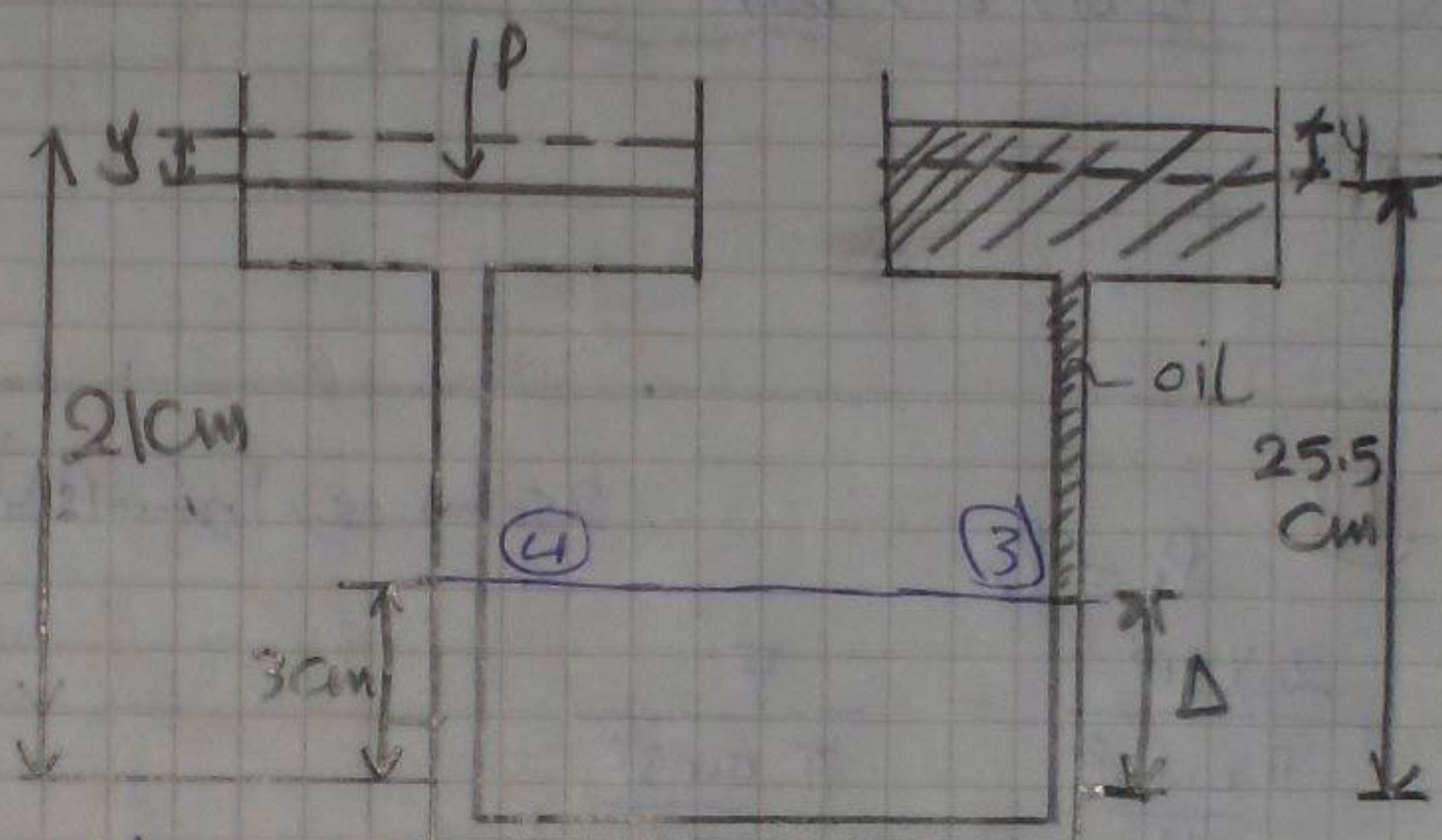
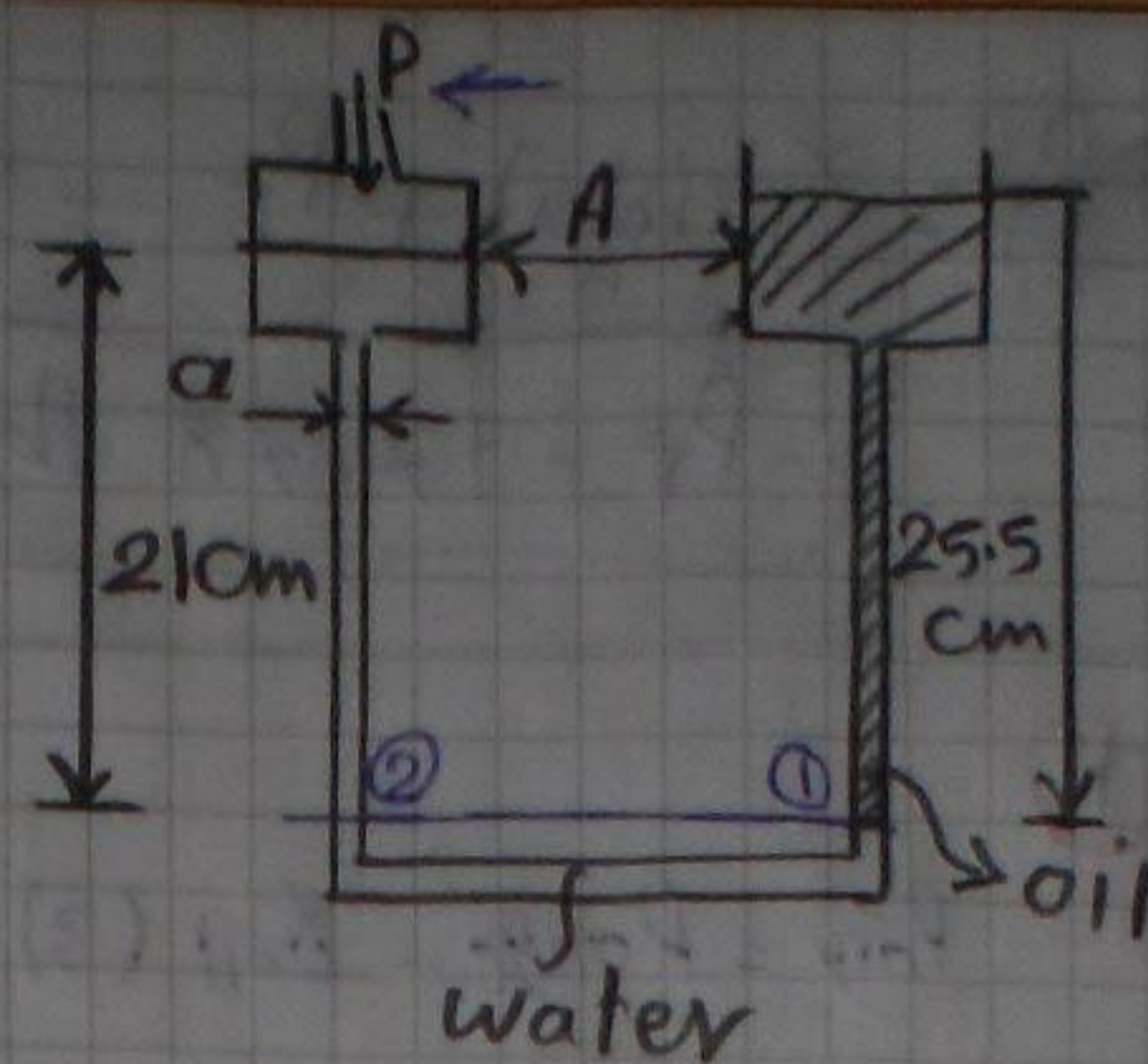
$$\therefore y = 6 \times 10^{-4} \text{ m}$$

$$P_3 = P_u$$

$$\therefore \gamma_{oil} (0.255 - 0.03 + 6 \times 10^{-4}) = \gamma_w (0.21 - 0.03 + 6 \times 10^{-4}) + P$$

$$1822.583 = 1759.914 + P$$

$$\therefore P = 62.669 \text{ Pa scal}$$



10  $P_A = 1.2 \text{ bar} = 1.2 \times 10^5 \text{ Pascal}$

$$P_B = P_A - \gamma_w (h) = 1.2 \times 10^5 - 9810 (0.4)$$

$$\therefore P_B = 116076 \text{ Pascal} = 1.16076 \text{ bar}$$

$$P_B = \frac{116076 (0.0254)^2}{4.44}$$

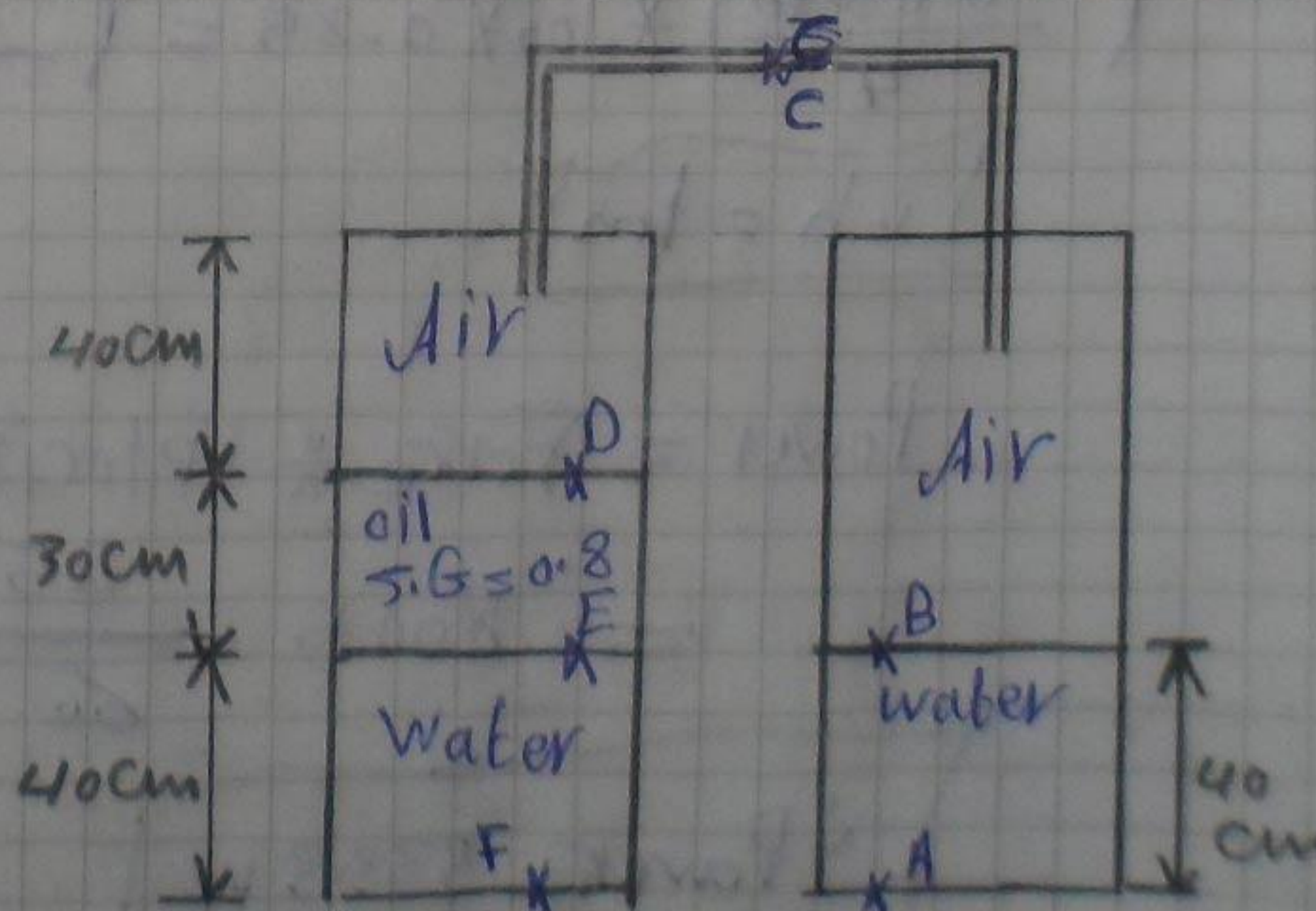
$$\therefore P_B = 16.87 \text{ lb/inch}^2$$

$$P = \gamma h \quad \therefore h = 38.81 \text{ ft}$$

$$P_B = P_C = P_D = 1.16076 \text{ bar} = 16.87 \text{ lb/inch}^2$$

$$P_E = \gamma_{oil} (0.3) + P_D = 0.8 \times 9810 \times 0.3 + 116076 = 118430 \text{ Pascal}$$

$$P_E = 1.18 \text{ bar} = 17.21 \text{ lb/inch}^2$$





$$P_T = \gamma_w(h_w) + P_E = 9810(0.4) + 118430 = 122354 \text{ Pascal}$$

$$\therefore P_T = 17.78 \text{ lb/inch}^2 = 1.22 \text{ bar}$$

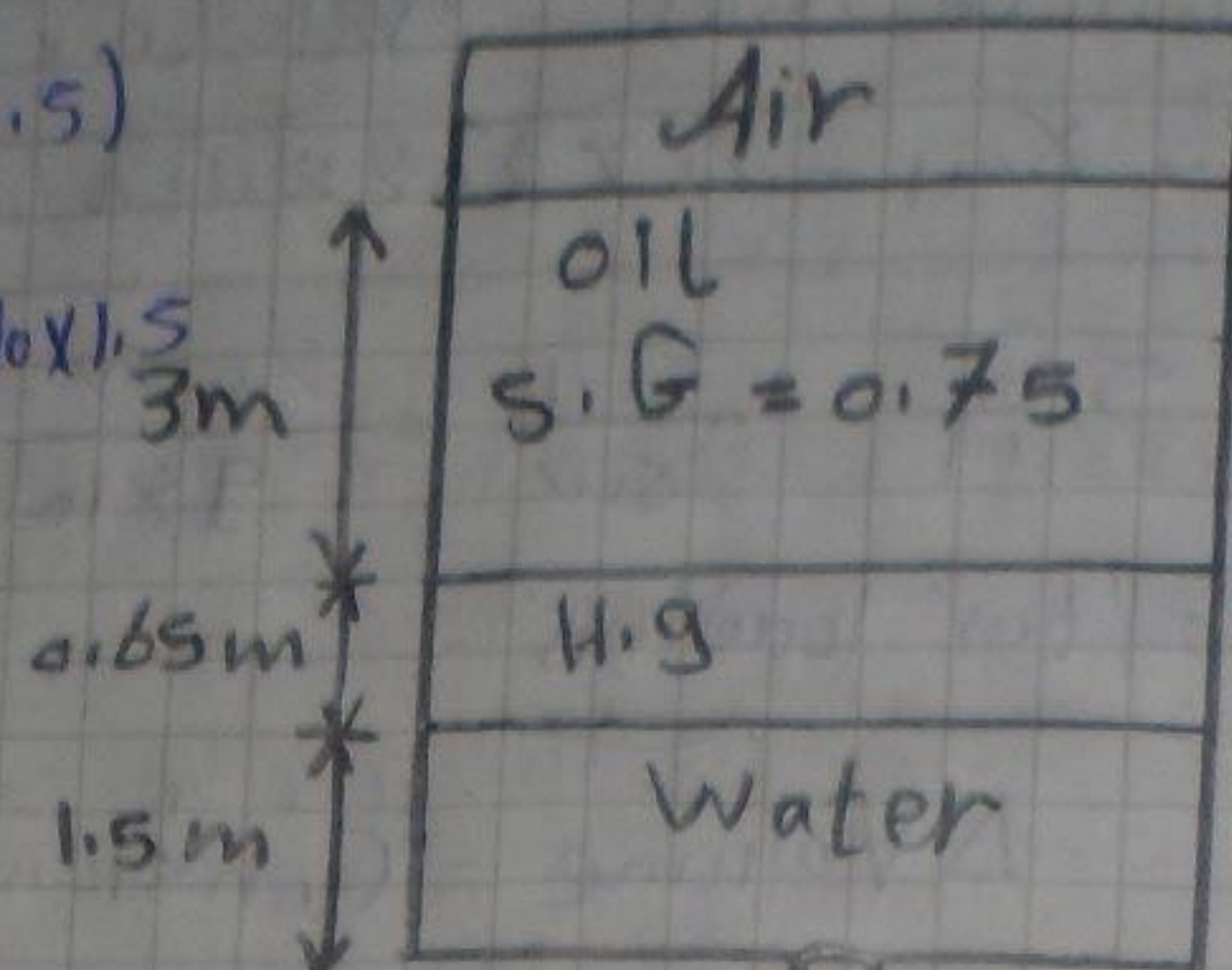
(11)

$$P_{air} = P_{gauge} - \gamma_{oil}(3) - \gamma_{Hg}(0.65) - \gamma_w(1.5)$$

$$P_{air} = 2 \times 10^5 - 0.75 \times 9810 \times 3 - 13600 \times 9.81 \times 0.65 - 9810 \times 1.5$$

$$\therefore P_{air} = 76492.1 \text{ Pascal}$$

$$= 0.765 \text{ bar}$$



$$P_{gauge} = 2 \times 10^5 \text{ bars}$$

(12)

$$P_1 = P_2$$

$$250 \text{ mm} = 19 \frac{1}{4} \text{ inch}$$

$$\frac{20 \times 10^3}{\pi \frac{0.15^2}{4}} = \frac{F}{\pi \frac{0.03^2}{4}}$$

$$\therefore F = 800 \text{ N}$$

$$V_d = V_u$$

السرعة في الدائرة = السرعة في الأنبوب

$$\left( \frac{0.03^2 \pi}{4} \right) \times 100 \times 0.25 = \left( \frac{0.15^2 \pi}{4} \right) h$$

$$\therefore h = 1 \text{ m}$$

$$\text{Power} = \text{Force} \times \text{Velocity}$$

$$= 800 \times \frac{25}{60}$$

$$\therefore \text{Power} = 333.3 \text{ W}$$

